

# **2019 IEEE 26th Symposium on Computer Arithmetic (ARITH 2019)**

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# 26th IEEE Symposium on Computer Arithmetic

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